

COMS30035, Machine learning: Combining Models 1, Selection

Edwin Simpson

`edwin.simpson@bristol.ac.uk`

Department of Computer Science, SCEEM
University of Bristol

November 14, 2023

Agenda

- ▶ **Model Selection**
- ▶ Model Averaging
- ▶ Ensembles: Bagging
- ▶ Ensembles: Boosting and Stacking
- ▶ Tree-based Models
- ▶ Conditional Mixture Models
- ▶ Ensembles of Humans

Textbook

We will follow Chapter 14 of the Bishop book: Bishop, C. M., Pattern recognition and machine learning (2006). Available for free [here](#).

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 - ▶ The features of the data used as inputs to the model;

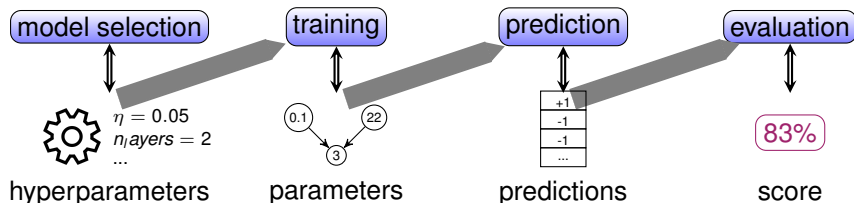
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 - ▶ Parameters of the learning algorithm, like learning rate for stochastic gradient descent (SGD);
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 - ▶ The examples in the dataset the model is trained on;
 - ▶ Random initialisation of parameters for EM or SGD

Hyperparameters



- ▶ It's useful to characterise all of these modelling decisions as *hyperparameters*
- ▶ Hyperparameters = all modelling choices that are fixed before training

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- ▶ Weakness: if the validation set is small, we might choose the wrong model!

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Dataset:

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Validation
/Development

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- ▶ Random search: test random combinations of hyperparameters
- ▶ Grid search: For each hyperparameter, define a set of values to test
 - ▶ Use your knowledge of the problem to test only reasonable values
 - ▶ For numerical hyperparameters, e.g., learning rate, choose a set of evenly-spaced values within a sensible range
 - ▶ H contains all combinations of the chosen hyperparameter values

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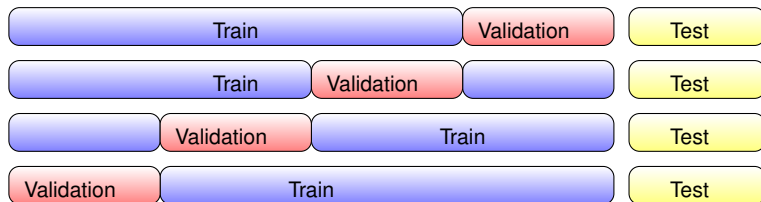
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 - ▶ Use your knowledge of the problem to test only reasonable values
 - ▶ For numerical hyperparameters, e.g., learning rate, choose a set of evenly-spaced values within a sensible range
 - ▶ H contains all combinations of the chosen hyperparameter values
- ▶ Reduce the number of tests needed to find a good combination using a more intelligent strategy such as Bayesian Optimisation

Cross-validation



- ▶ Split the training data into k random, equally-sized subsets;
- ▶ For each of the k folds: leave out the k th subset from training, train on the rest and test on the k th subset;
- ▶ Compute the average performance across all k folds;
- ▶ Avoids overfitting by tuning on training set performance...
- ▶ And avoids tuning on a single small validation set.

Now do the quiz!

Please do the quiz for this lecture on Blackboard.